Transformers

Where $I_1 =$ Primary current

 I_2 = Secondary current

Transformation ratio $a = \frac{V_1}{V_2} = \frac{E_1}{E_2} = \frac{N_1}{N_2} = \frac{I_2}{I_1}$

The phasor diagram of ideal transformer is as below:



CURRENT, VOLTAGE AND IMPEDANCE REFERRED TO PRIMARY SIDE

Secondary voltage referred to primary side.

$$V_2' = \left(\frac{N_1}{N_2}\right) V_1$$

Secondary load current referred to primary side.

$$I_2' = \left(\frac{N_2}{N_1}\right) I_1$$

Secondary impedance referred to primary side.

$$Z_2' = \left(\frac{N_1}{N_2}\right)^2 Z_2$$

$$\overline{I}_{a} r_{a} = 0.02 \quad (0.8 - j \ 0.6)$$

$$\overline{I}_{a} r_{a} = 0.016 - j \quad 0.012$$
Applying the relation. $E'_{f} = \overline{V}_{I} + j \overline{I}_{a} X_{q} - \overline{I}_{a} r_{a}$

$$= 1 + 0.48 + j \ 0.64 + 0.016 - j \ 0.012$$

$$= 1.496 + j \ 0.532 = 1.588 \angle 19.58$$

$$\therefore \qquad \text{Load angle} = 19.58^{\circ}$$

$$\therefore \qquad \delta + \theta = 19.58^{\circ} + 36.9^{\circ} = 56.48^{\circ}$$
We have $I_{d} = I_{a} \sin(\delta + \theta) = 1.00 \sin 56.48^{\circ} = 0.834 \text{ pu}$

$$I_{q} = I_{a} \cos(\delta + \theta) = 1.00 \cos 56.48 = 0.552 \text{ pu}$$
To calculate excitation $E_{f} = E'_{f} + I_{d} (x_{d} - x_{q})$

$$= 1.588 + 0.834 \times 0.2 = 1.755 \text{ Ans.}$$

$$\overline{E}_{f} = 1.755 \angle 19.58^{\circ} \text{ pu} \text{ Ans.}$$

Problem 5.39 : A 25 MVA, 3-phase star-connected alternator, with an impedance of 6 Ω and a resistance of 0.4 Ω is operating in parallel with constant voltage 10 kV bus bars. If its field is adjusted to give an excitation voltage of 11 kV. Calculate

- (a) The maximum power output from the alternator
- (b) The armature current and power factor under maximum power condition.

Solution :

Given,
$$E_f = 11 \text{ kV}, V_f = 10 \text{ kV}, Z_s = 6 \Omega, r_a = 0.4 \Omega$$

Alternator excitation/phase

$$\frac{11000}{\sqrt{3}} = 6351 \text{ V}$$

Alternator terminal voltage/phase = $\frac{10000}{\sqrt{3}}$ = 5774 V

(a) To calculate maximum power, Applying the relation

$$P_{o\max} = \frac{E_f V_t}{Z_s} - \frac{V_t^2}{Z_s^2} \times r_a = \frac{5774 \times 6351}{6} - \frac{(5774)^2}{36} \times 0.4$$

= 5741344.8 = 5.7 MW/phase
= 17.1 MW for line **Ans.**

Now, Slip (s) =
$$\frac{\text{Rotor copper loss}}{\text{Power across air gap}} = \frac{3}{86.5} = 0.0347$$
 Ans.

Problem 6.9 : The power supplied to a 3-phase induction motor is 40 kW and the corresponding stator losses are 1.5 kW. Calculate the net mechanical power developed and the rotor $I^2 R$ loss when the slip is 0.04 per unit. What will be the net power developed if the speed of the above motor is reduced to 40 % of the synchronous speed by means of external rotor resistors, assuming the torque and stator losses to remain unaltered? Friction and windage losses may be assumed to be 0.8 kW. (*I.A.S.*, 1980)

Solution :

Let un choose 40 kW as base power and speed 1500 rpm as base synchronous speed

Power input, $p_i = \frac{40}{40} = 1.00$ p.u. *.*.. Synchronous speed $(n_s) = \frac{1500}{1500} = 1$ p.u., slip = 0.04 Stator losses in p.u. = $\frac{\text{Stator losses}}{\text{base power}} = \frac{1.5}{40} = 0.0375 \text{ p.u.}$ Friction and windage losses = $\frac{0.8}{40} = 0.02 \text{ p.u.}$ Now, Power across air gap, $p_G = p_{in}$ - Stator losses = 1 - 0.0375 = 0.9625 p.u. Rotor copper loss = $s \times p_G = (0.04 \times 0.9625)$ p.u. = 0.0385 Net power output $P_{net} = p_G - rotor loss - windage and friction loss$ = 0.9625 - 0.0385 - 0.02 = 0.904 p.u. Actual power developed = Power in p.u. $\times P_{base}$ $= 40 \times 0.904 = 36.16$ kW Ans. Rotor speed $(n_r) = (1 - s) n_s = (1 - 0.04) \times 1 = 0.96$ p.u. Actual speed of the rotor $= 0.96 \times \text{base speed}$ $= 0.96 \times 1500 = 1440$ rpm When the speed is reduced to 40 % of synchronous speed

Problem 6.13 : The maximum torque of a 3-phase squirrel-cage induction motor is 4 times the full-load torque and the starting torque is 1.6 times the full-load torque. Neglect stator resistance. Calculate (i) The slip at the maximum torque

- (ii) Full-load slip and
- (iii) The rotor current at starting in terms of full-load rotor current.

Solution :

Given,

$$T_{\text{max}} = 4 \times T_{fl}$$

and

- $T_{st} = 1.6 \times T_{fl}$
- (i) Applying the relation,

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$$\frac{T_{st}}{T_{\max}} = \frac{2}{\frac{s_{\max,T}}{1} + \frac{1}{s_{\max,T}}}$$

or

$$\frac{.6 T_{fl}}{4 T_{fl}} = \frac{2 s_{\max, T}}{s_{\max, T}^2 + 1}$$

or

$$=\frac{2 s_{\max, T}}{s_{\max, T}^2 + 1}$$

or
$$s_{\max, T}^2 - \frac{2}{0.4} s_{\max, T} + 1 = 0$$

0.4

or
$$s_{\max, T}^2 - 5 s_{\max, T} + 1 = 0$$

This yields
$$s_{\max, T} = \frac{5 \pm \sqrt{25 - 4}}{2}$$

$$=\frac{5\pm 4.5826}{2}$$

Neglective higher value, $s_{max, T} = 0.21$ Ans. (*ii*) To calculate full load slip, Applying the relation,

$$\frac{T_{fl}}{T_{\max}} = \frac{2}{\frac{s_{fl}}{\frac{s_{fl}}{s_{\max,f}} + \frac{s_{\max,f}}{s_{fl}}}}$$